

[more quarks]

(20) MQ-1

[About 1965] Leptons ν_e ν_μ
 e^- μ^-

Quarks u
 d s

Glashow proposed a new "charmed" quark c [wouldn't it be charming?]
 w/ a property called charm C

[Nov 1974] New meson discovered ψ / $m \sim 3000 \text{ MeV}$ [$\rightarrow$ see plot.]

called $\begin{cases} \psi & [\text{SLAC, Richter}] \\ J & [\text{BNL, Ting}] \end{cases}$

$\downarrow$ [PPB, toward end of mesons, p. 116 in 2018 edition]
 $J/\psi = \text{charmonium} = c\bar{c}$ $m \sim 3100 \text{ MeV}$

$$\Rightarrow m_c \sim 1500 \text{ MeV}$$

Other charmed mesons soon discovered

$$\begin{aligned} D^+ &= c\bar{d} \\ D^0 &= c\bar{u} \end{aligned} \quad \left. \vphantom{\begin{aligned} D^+ &= c\bar{d} \\ D^0 &= c\bar{u} \end{aligned}} \right\} m \sim 1900 \text{ MeV}$$

$$D_s^+ = c\bar{s} \quad m \sim 2000 \text{ MeV}$$

Charmed baryons

Step 3: baryons

$$\begin{aligned} \Sigma_c^{++} &= c u u \\ \Lambda_c^+ &= c u d \\ \Sigma_c^0 &= c d d \\ \Sigma_c^{++} &= c c u \\ \Sigma_c^+ &= c c d \quad \text{and} \quad \Sigma_{ccc}^{++} = c c c \end{aligned} \quad \left[\begin{array}{l} \text{analogous to} \\ \Sigma \sim \begin{matrix} s u u \\ s u d \\ s d d \end{matrix} \end{array} \right]$$

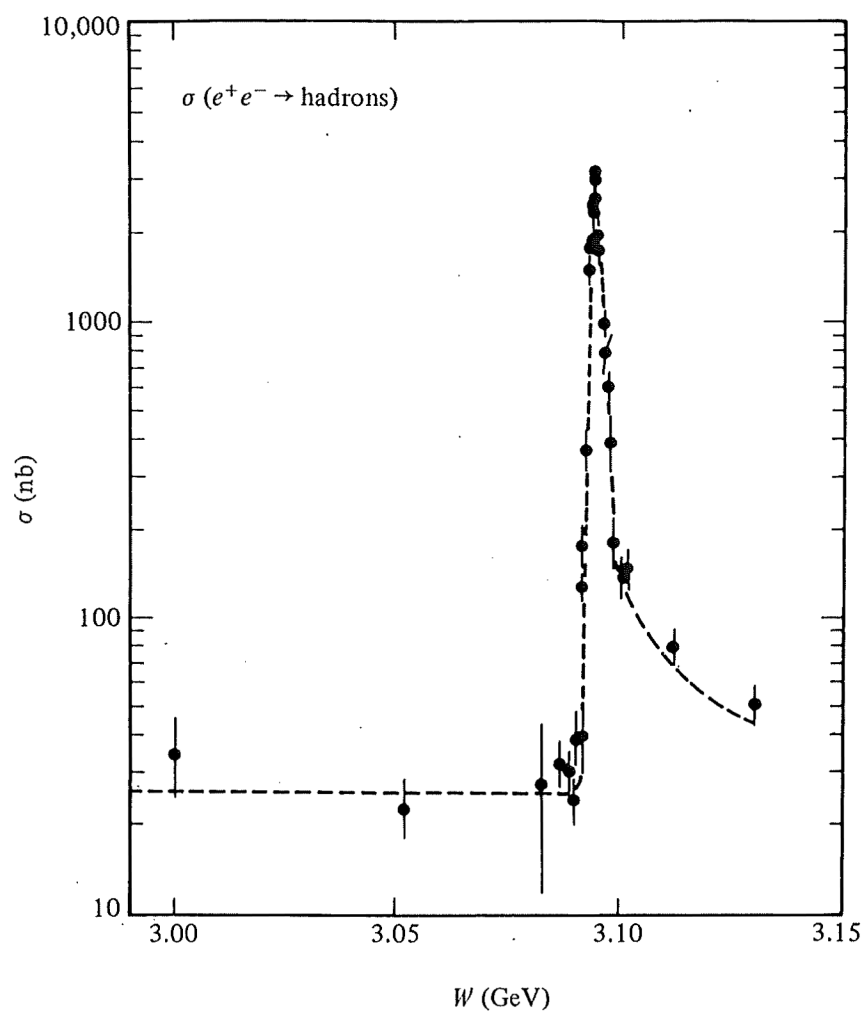
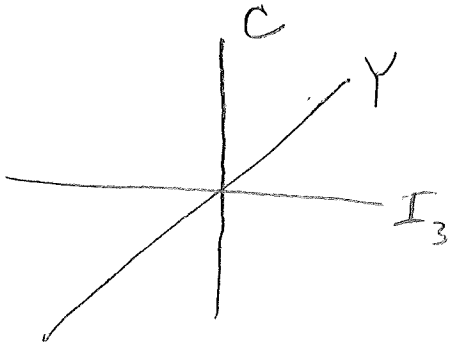


Fig. 10.23. Total hadron production cross section in e^+e^- collisions near 3.1 GeV and the J/ψ peak. [From A. M. Boyarski et al., *Phys. Rev. Lett.* **34**, 1357 (1975).]

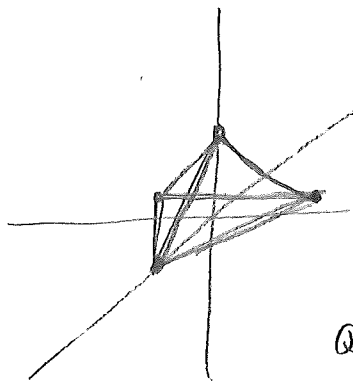
[New quantum number $\Rightarrow$ another dimension to weight diagram]



Use hypercharge Y instead of S

$$Y = S + A - \frac{1}{3}C$$

	I_3	A	S	C	Y
u	$\frac{1}{2}$	$\frac{1}{3}$	0	0	$\frac{1}{3}$
d	$-\frac{1}{2}$	$\frac{1}{3}$	0	0	$\frac{1}{3}$
c	0	$\frac{1}{3}$	0	1	0
s	0	$\frac{1}{3}$	-1	0	$-\frac{2}{3}$



tetrahedron

Quarks belong to $\underline{4}$ of $SU(4)$

Mesons belong to $\underline{4} \otimes \overline{\underline{4}} = \underline{15} \oplus \underline{1}$
 $\uparrow$
 cuboctahedron

baryons belong to $\underline{4} \otimes \underline{4} \otimes \underline{4} = \underline{20} \oplus \underbrace{\underline{20}_s \oplus \underline{20}_a}_{\text{truncated pyramids}} \oplus \overline{\underline{4}}$
 $\uparrow$ pyramid $\uparrow$ inverted tetrahedron

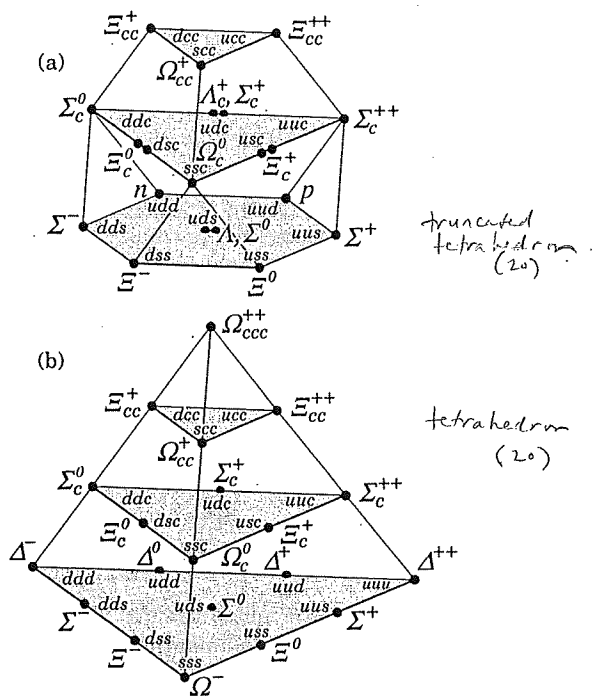


Figure 14.4: SU(4) multiplets of baryons made of u , d , s , and c quarks. (a) The 20-plet with an SU(3) octet. (b) The 20-plet with an SU(3) decuplet.

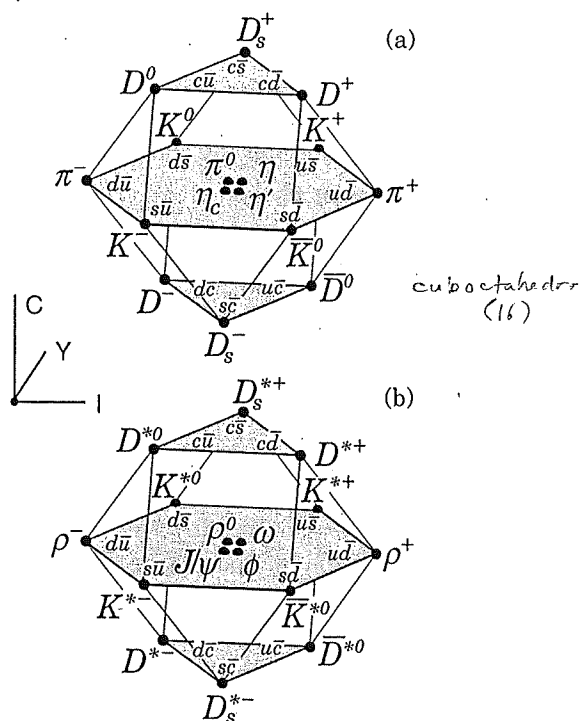


Figure 14.1: SU(4) weight diagram showing the 16-plets for the pseudoscalar (a) and vector mesons (b) made of the u , d , s and c quarks as a function of isospin I , charm C and hypercharge $Y = S+B - \frac{C}{3}$. The nonets of light mesons occupy the central planes to which the $c\bar{c}$ states have been added.

$$\Sigma_c^+, \Lambda_c^+ \quad uuc \quad d$$

$$\Sigma_c^{++} \quad uuu$$

$$\Sigma_c^0 \quad cdd$$

$$\Xi_{cc}^{++} \quad ccu$$

$$\Xi_{cc}^+ \quad ccd$$

$$\Omega_{ccc}^{++} \quad ccc$$

$$\begin{array}{ll} D^0 & c\bar{u} \\ D^+ & c\bar{d} \\ D_s^+ & c\bar{s} \end{array} \quad (1976)$$

Third generation

ν_e	ν_μ	ν_τ	(disc 1999)	
e^-	μ^-	τ^-	(disc 1975)	top/bottom
u	c	t	(disc 1994)	truth/beauty
d	s	b	(disc 1977)	

(1977) $\Upsilon = \text{upsilon} = \text{bottomium } b\bar{b}$ $m \sim 10 \text{ GeV} \Rightarrow m_b \sim 5 \text{ GeV}$

(1983) B-mesons: contain one b or $\bar{b}$ [analogous to K's, D's]

$$B^+ = u\bar{b}$$

$$B^0 = d\bar{b}$$

$$B_s^0 = s\bar{b}$$

$$B_c^+ = c\bar{b} \text{ etc.}$$

Beautiful baryons

(1981) $\Lambda_b = udb$

Top quark, long anticipated, not disc. until 1994 at Fermilab

Decays so quickly that no mesons are formed

$$\Gamma \sim 1.4 \text{ GeV} \Rightarrow 5 \times 10^{-25} \text{ s} \ll 10^{-23} \text{ s}$$

Why such a wide range of quark masses?

Why 3 generations?