# **Motion Planning:**

#### A Journey of Robots, Digital Actors, Molecules and Other Artifacts

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#### My Research Interests

- Autonomous agents that sense, plan, and act in real and/or virtual worlds
- Algorithms and systems for representing, capturing, planning, controlling, and rendering motions of physical objects
- Applications:
  - Manufacturing
  - Mobile robots
  - Computational biology
  - Computer-assisted surgery
  - Digital actors

#### Goal of Motion Planning

- Compute motion strategies, e.g.:
  - geometric paths
  - time-parameterized trajectories
  - sequence of sensor-based motion commands
- To achieve high-level goals, e.g.:
  - go to A without colliding with obstacles
  - assemble product P
  - build map of environment E
  - find object O

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# Examples





## Is It Easy?







#### **Basic Problem**

#### • Statement:

Compute a collision-free path for a rigid or articulated object (the robot) among static obstacles

#### Inputs:

- Geometry of robot and obstacles
- Kinematics of robot (degrees of freedom)
- Initial and goal robot configurations (placements)

#### Outputs:

 Continuous sequence of collision-free robot configurations connecting the initial and goal configurations

## Example with Rigid Object



## Example with Articulated Object



#### Extensions to the Basic Problem

- Moving obstacles
- Multiple robots
- Movable objects
- Deformable objects
- Goal is to gather data by sensing

- Nonholonomic constraints
- Dynamic constraints
- Optimal planning
- Uncertainty in control and sensing

## Application: Design for Manufacturing









## **Application: Robot Programming and Placement**





David Hsu's PhD

## Application: Checking Building Code



Charles Han's PhD

## Application: Generation of Instruction Sheets



## Application: Model Construction by Mobile Robot



Hector Gonzalez' s PhD





## Application: Graphic Animation of Digital Actors



## **Application:** Computer-Assisted Surgical Planning





Rhea Tombropoulos' s PhD



Joel Brown's PhD

## Application: Prediction of Molecular Motions







Amit Singh's PhD

# Motion in Configuration Space



$$Q(t) = \begin{bmatrix} q_0(t) \\ \vdots \\ q_n(t) \end{bmatrix}$$
$$t \in [0, T]$$
$$\frac{\text{Parts DOF}}{L \begin{bmatrix} 19 & 68 \\ 51 & 118 \end{bmatrix}}$$

## Disc Robot in 2-D Workspace



## Rigid Robot Translating in 2-D

 $CB = B \Theta A = \{b - a \mid a \text{ in } A, b \text{ in } B\}$ 



## Rigid Robot Translating and Rotating in 2-D



## C-Obstacle for Articulated Robot



#### **Other Representation Concepts**

- State space (configuration x velocity)
- Configuration/state x time space
- Composite configuration/state spaces
- Stability regions in configuration/state spaces
- Visibility regions in configuration/state spaces
- ♦ Etc ...

#### Motion Planning as a Computational Problem

• Goal:

Compute the connectivity of a space (e.g., the collision-free subset of configuration space)

- High computational complexity: Typically requires time exponential in an input parameter, e.g., the number of degrees of freedom, the number of moving obstacles, ...
- Two main algorithmic approaches:
  - Planning by random sampling
  - Planning by computing criticalities

## Motion Planning as a Computational Problem

- Goal: Characterize the connectivity of a space (e.g., the collision-free subset of configuration space)
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## Motion Planning as a Computational Problem

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# Principle of Randomized Planning

(Probabilistic Roadmap)



## Why Does it Work?

[Kavraki, Latombe, Motwani, Raghavan, 95]



#### In Theory, a PRM Planner ...

- Is probabilistically complete, i.e., whenever a solution exists, the probability that it finds one tends toward 1 as the number N of milestones increases
- Under rather general hypotheses, the rate of convergence is exponential in the number N of milestones, i.e.:

Prob[failure]  $\sim \exp(-N)$ 

#### In practice, PRM Planners ...

Are fast

- Deal effectively with many-dof robots
- Are easy to implement
- Have solved complex problems



## Example 1: Planning of Manipulation Motions



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#### Example 2: Air-Cushioned Robot





## Example 3: Radiosurgical Planning



Cyberknife (Neurosurgery Dept., Stanford, Accuray)



## Surgeon Specifies Dose Constraints



#### **Beam Selection Algorithm**

- Place points uniformly at random on the surface of the tumor
- Pick beam orientations at random at these points



## **Beam Selection Algorithm**

- Place points uniformly at random on the surface of the tumor
- Pick beam orientations at random at these points



## Compute Beam Weights



2000 < Tumor < 2200 2000 < B2 + B4 < 2200 2000 < B4 < 2200 2000 < B3 + B4 < 2200 2000 < B3 < 2200 2000 < B1 + B3 + B4 < 2200 2000 < B1 + B4 < 2200 2000 < B1 + B4 < 2200 2000 < B1 + B2 + B4 < 2200 2000 < B1 + B2 + B4 < 2200 2000 < B1 + B2 + B4 < 2200 2000 < B1 + B2 + B4 < 2200

• 0 < Critical < 500 0 < B2 < 500

•

### **Sample Case**





#### Linac plan 80% Isodose surface

#### **CARABEAMER' s plan** 80% Isodose surface

## Sample Case



#### 50% Isodose Surface

80% Isodose Surface



CARABEAMER's plan

## Example 4: Indoor Map Building by Robot







# Next-Best View Strategy



## **Computing Next Sensing Position**

Sample the free edges of the visited region at random. For each sample point, compute the subset of visited region from which this point is visible and sample this subset at random.
Set of candidate positions q



- Select "best" candidate *q* based on following criteria:
  - overlap of visible environment edges (to ensure reliable alignment)
  - amount of potential new space visible from q
  - length of path to go to q

## Map Construction Example



## Robotics Lab Map



## Example 5: Digital Actor with Vision Sensing



#### Example 5: Digital Actor with Vision Sensing

#### Fast Path Planning for Perception-Based Navigation

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## **Example 6: Predicting Molecule Docking Motions**



## Future Work: Minimally Invasive Surgey Amidst Soft Tissue Structures





#### Future Work: Autonomous Interactive Characters



A Bug's Life (Pixar/Disney)



Toy Story (Pixar/Disney)



Antz (Dreamworks)



Tomb Raider 3 (Eidos Interactive)



The Legend of Zelda (Nintendo)



Final Fantasy VIII (SquareOne)

## Future Work: Protein Folding



#### Summary/Conclusion

- Over the last decade there has been considerable progress in motion planning techniques and their application
- While motion planning originated in robotics, the areas of application are now very diverse: product design, manufacturing, graphic animation, video games, biology, etc...
- There are orders of magnitude more processors embedded in physical devices (cars, planes, surgical instruments, etc) than desktop computers, and the gap is still growing. The interest in modeling and computing the motion of physical objects will continue to grow.