

csci 210: Data Structures

Sorting

Problem

- Input: an array of elements that can be compared to each other
 - $A = [x_1, x_2, x_3, \dots, x_n]$
- Output:
 - a new array B that contains the elements in A in increasing order
 - $B[0] \leq B[1] \leq B[2] \dots$
 - or the same array A, rearranged so that the elements are in increasing order
 - $A[0] \leq A[1] \leq A[2] \dots$
- Permuting the input array is advantageous because it does not use extra space (memory).
- A sorting algorithm that permutes the input array and does NOT create a new output array is called "in-place"

Sorting algorithms

▪ Bubble-sort

- idea: a pass through the array swaps elements that are out-of-order
- need $n-1$ passes in the worst-case
- analysis: $O(n^2)$, in-place

▪ Insertion sort

- idea: the elements processed so far are kept in order. take the next element in the input and insert it in the right spot in the sorted array.
- analysis: $O(n^2)$, in-place

▪ Selection sort

- idea: select the smallest, put it in position 0; select the next smallest, put it in position 1, and so on.
- analysis: $O(n^2)$, in-place

▪ Mergesort

- idea: split into 2 halves. sort each half recursively. merge.
- analysis: $O(n \lg n)$, not in-place

← no proof here [in csci 231]

▪ Quicksort

- idea: pick an element and call it pivot. re-arrange the input so that all element \leq pivot are to its left, and all element $>$ pivot are to its right. sort each part recursively. no need of merging.
- analysis: $O(n^2)$, in-place

← no proof here [in csci 231]